

PROCEEDINGS
OF THE
AMERICAN MATHEMATICAL SOCIETY

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Bulletin of the American Mathematical Society

This journal is the official organ of the Society. It reports official acts of the Society and the details of its meetings. It contains some of the officially invited addresses presented before the Society, reviews of advanced mathematical books, research problems and a department of research announcements.

One volume of six numbers is planned for 1965.

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CONTENTS

Vol. 16, No. 2

APRIL, 1965

Whole No. 92

	Page
Embedding punctured manifolds. By D. B. A. EPSTEIN	175
An extension of the concept of L_n sets. By J. W. MCCOY	177
The collineation groups of free planes. II: A presentation for the group G_2 . By REUBEN SANDLER	181
Pseudo-isotopically contractible spaces. By O. G. HARROLD, JR.	186
On a problem of Grünbaum. By J. G. CEDER	188
A new proof of Deicke's theorem on homogeneous functions. By F. BRICKELL	190
Free groups and handlebodies. By J. J. ANDREWS AND M. L. CURTIS	192
Strong ratio limit property for R -recurrent Markov chains. By W. E. PRUITT	196
A representation theorem for continuous functions of several variables. By D. A. SPRECHER	200
Decompositions and reflexivity in Banach spaces. By B. L. SANDERS	204
Ideals of square summable power series. II. By JAMES ROVNYAK	209
More about invertible operators without roots. By J. J. SCHÄFFER	213
A geometric proof of the Lebesgue differentiation theorem. By DONALD AUSTIN	220
Uniform integrability and the pointwise ergodic theorem. By YUJI ITO	222
Holomorphic imprimitivities. By P. C. DELIYANNIS	228
On wandering subspaces for unitary operators. By J. B. ROBERTSON	233
Subspaces of $C(H)$ which are direct factors of $C(H)$. By D. W. DEAN	237
The derivative of a monotonic discontinuous function. By G. PIRANIAN	243
Stationary measures for branching processes. By J. F. C. KINGMAN	245
The coefficients in an asymptotic expansion. By L. CARLITZ	248
On classes of univalent continued fractions. By T. L. HAYDEN and E. P. MERKES	252
A remark concerning Littlewood's Tauberian theorem. By H. S. SHAPIRO	258
Variations on a theme of Widder. By E. R. LOVE	260
The maximum term of an entire series with gaps. By J. D. BUCKHOLTZ	272
Mixed boundary-value problems in the plane. By J. A. VOYTUK and R. C. MAC CAMY	276
On the zeros of a confluent hypergeometric function. By JET WIMP	281
A note on multivalent starlike functions. By A. W. GOODMAN and J. A. HUMMEL	284
An extension of Tate's theorem on cohomological triviality. By L. EVENS	289
Quasi-invertible prime ideals. By H. S. BUTTS	291
A particular class of Lie algebras. By G. LEGER	293
On the line graph of a projective plane. By A. J. HOFFMAN	297
The polynomial of a directed graph. By A. J. HOFFMAN and M. H. McANDREW	303
An inequality on doubly stochastic matrices. By C. J. EVERETT	310
Perfect closures of rings and schemes. By M. J. GREENBERG	313
On matrices whose real linear combinations are nonsingular. By J. F. ADAMS, P. D. LAX and R. S. PHILLIPS	318
On the indecomposability of torsion-free abelian groups. By J. W. ARMSTRONG	323
A class of simple lattice-ordered groups. By CHARLES HOLLAND	326
Bounds for pairs of cubic residues. By M. DUNTON	330

SHORTER NOTES

A simple proof of Jacobi's triple product identity. By G. E. ANDREWS	333
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