

PROCEEDINGS  
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## Proceedings of the American Mathematical Society

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\* The volume index will contain a mapping showing the correspondence between sections A-G and the AMS subject classification numbers.