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[^1]:    * The volume indexes contain a mapping showing the correspondence between sections A-G and the AMS (MOS) subject classification numbers.

