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This journal is the official organ of the Society. It reports official acts of the Society and the details of its meetings. It contains some of the officially invited addresses presented before the Society, reviews of advanced mathematical books, and a department of research announcements.

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Mathematics of the USSR—Sbornik

This journal is a cover-to-cover translation of MATEMATIČESKIĬ SBORNIK (New Series), published monthly by the Moscow Mathematical Society and the Academy of Sciences of the USSR. It is a journal of current research in all fields of pure mathematics. The translation is published monthly starting with Volume 1, Number 1, January 1967.

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Send papers directly to one of the editors listed under the subject field of the paper.

Algebra and algebraic number theory.

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Modern or classical analysis and analytic number theory.

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Algebraic geometry.

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Set-theoretic and general topology.

THOMAS A. CHAPMAN, Department of Mathematics, University of Kentucky, Lexington, Kentucky, 40506

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Algebraic topology and all other types of geometry.

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ROBERT I. SOARE, Department of Mathematics, University of Illinois at Chicago Circle, Chicago, Illinois 60680

Combinatorics and related areas of discrete mathematics.

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