# **PROCEEDINGS**

OF THE

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### Proceedings of the American Mathematical Society

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#### Submission of Manuscript

Send papers directly to one of the editors listed under the subject field of the paper.

Algebra and algebraic number theory.

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Algebraic geometry.

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Set-theoretic and general topology.

THOMAS A. CHAPMAN, Department of Mathematics, University of Kentucky, Lexington, Kentucky 40506

W. WISTAR COMFORT, Department of Mathematics, Wesleyan University, Middletown, Connecticut 06457

Algebraic topology and all other types of geometry.

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Applied mathematics, differential equations, and related areas of analysis.

FRED G. BRAUER, Department of Mathematics, University of Wisconsin, Madison, Wisconsin 53706

Probability, statistics, and related fields.

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Logic, set theory, and related areas.

ROBERT I. SOARE, Department of Mathematics, University of Illinois at Chicago Circle, Chicago, Illinois 60680

Combinatorics and related areas of discrete mathematics.

JAY R. GOLDMAN, School of Mathematics, University of Minnesota, Minneapolis, Minnesota 55455

All other communications should be addressed to the Managing Editor, JOSEPH J. ROTMAN, at the above address.

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## CONTENTS—Continued from back cover

Shocks violating Lax's condition are unstable. By E. D. Conway and J. A. SMOLLER	353 357
D. Geometry	
Families of negatively curved hermitian manifolds, By MICHAEL J. COWEN	362
Criteria for unique metric lines in Banach spaces. By E. Z. Andalafte and J. E. Valentine	367
E. LOGIC AND FOUNDATIONS	
Effective matchmaking and k-chromatic graphs. By Alfred B. Manaster and Joseph G. Rosenstein.	371
G. Topology	
A generalization of the dog bone space to $E^n$ . By W. T. EATON	379 388 395 402
potent Lie groups. By Roe Goodman	409 414
On the reduction of complex bordism to unoriented bordism. By DAVID COPELAND JOHNSON	417
A topological proof of a theorem of Kneser. By BJORN FRIBERG	421
and Leonard R. Rubin	427 433
Open simple maps and periodic homeomorphisms. By John D. Baildon  A metric characterizing Čech dimension zero. By K. A. Broughan  Peripherally compact tree-like spaces are continuum-wise connected. By Ralph	433
Bennett	441

## **CONTENTS\***

Vol. 39, No. 2

**JULY 1973** 

Whole No. 169

	Page
A. Algebra and Number Theory	
Free derivation modules and a criterion for regularity. By Selmer Moen  A group of exponent 4 with derived length at least 4. By S. BACHMUTH, H. Y.	221
Mochizuki and K. Weston. Every $n \times n$ matrix Z with real spectrum satisfies $  Z-Z^*   \le   Z+Z^*   (\log_2 n + \log_2 n)$	228
O.038). By W. Kahan	235
Regular P.Irings. By E. P. Armendariz and Joe W. Fisher.  Lattice sums of homogeneous functions. By ROBERT S. CAHN	247 252
The ring of polynomials over a von Neumann regular ring. By P. J. McCarthy A class of partially ordered linear algebras. By RALPH DEMARR	253 255
A two-color theorem for analytic maps in $R^n$ . By Bryan E. Cain	261
Strict radical classes of associative rings, By Patrick N, Stewart	267 273
By Adolf Miklave	279
B. Analysis	
Distortion theorems for a special class of analytic functions. By DOROTHY BROWNE	
SHAFFER	281
functions." By Alan L. Schwartz	288
variant spaces. By Kenneth F. Andersen	295 300
functions. By Su-shing Chen	305
An extremal problem for the geometric mean of polynomials. By E. Beller and	308
D. J. Newman An alternate characterization of continuity. By BRUCE D. SMITH	318
On the growth of the Taylor coefficients of automorphic forms. By Thomas A. Metzger	321
Asymptotic inversion of Laplace transforms: A class of counterexamples. By JOHN S. Lew	329
Dirichlet problems for singular elliptic equations. By CHI YEUNG LO	337
RADIN	343
Convolutions and absolute continuity. By D. A. LIND	347
Charles K, Chui	349

<sup>\*</sup> The volume indexes contain a mapping showing the correspondence between sections A-G and the AMS (MOS) subject classification numbers.