

## ERRATUM TO "GENERALIZED RELATIVE DIFFERENCE SETS"

CLEMENT W. H. LAM AND STANLEY E. PAYNE

**ABSTRACT.** This note gives the correction of a theorem previously published. A counterexample is also given for the theorem as originally stated.

In [1], a nonexistence theorem was given for a normal  $(0, 1)$ -matrix  $A$  with three distinct characteristic roots such that  $A^T A = c_0 I - c_1 (I_m \otimes J_n)$ . However, part (i) of Theorem 1.5 as stated is incorrect. A counterexample is the cyclic relative difference set  $R(13, 2, 9, 3)$  whose elements are  $\{2, 4, 6, 7, 10, 11, 12, 18, 21\}$ . For this set,  $m$  is odd and the Hilbert symbol  $(3, 26)_3 = -1$ .

In the notation of [1], let  $W_1$  be the space of characteristic (column) vectors of  $B = A^T A$  associated with  $\theta_1 = c_0 - nc_1$ . For  $1 \leq j < m$ , let  $\alpha_j$  be the vector of size  $mn$  with  $+1$  in positions  $1, 2, \dots, n$ , with  $-1$  in positions  $jn+1, \dots, jn+n$ , and with zeros elsewhere. Then  $\{\alpha_j | j = 1, \dots, m-1\}$  is a basis for  $W_1$ . Let  $G = ((\alpha_i, \alpha_j))_{1 \leq i, j \leq m-1}$ . Then  $G = n(I_{m-1} + J_{m-1})$ . Thus  $q_1 = \det G = n^{m-1}m$ , instead of  $q_1 = mn$  as stated in [1]. Hence Theorem 1.5(i) should read: If  $m$  is odd, then  $(c_0 - nc_1, (-1)^{(m-1)/2}m)_p = +1$  for all primes  $p$ .

The Bruck-Ryser Theorem applied to  $A^*$  (see [1, Theorem 1.6]) says in this case that  $(c_0 - nc_1, (-1)^{(m-1)/2}nc_1)_p = +1$  for all primes  $p$ . These two conditions are equivalent if and only if  $(c_0 - nc_1, mnc_1)_p = +1$  for all primes  $p$ . But  $c_0 - nc_1 = c_0^2 - mnc_1$ . Put  $x = 1/c_0 = y$ . Then  $x^2(c_0^2 - mnc_1) + y^2(mnc_1) = 1$ , implying that  $(c_0 - nc_1, mnc_1)_p = +1$  for all primes  $p$ . Hence the Bruck-Ryser Theorem applied to  $A^*$  is indeed equivalent to the correct form of Theorem 1.5(i).

### REFERENCES

1. S. E. Payne, *Generalized relative difference sets*, Proc. Amer. Math. Soc. **25** (1970), 46–50. MR 40 #7134.

COMPUTER SCIENCE DEPARTMENT, CONCORDIA UNIVERSITY, MONTREAL, QUEBEC, CANADA

DEPARTMENT OF MATHEMATICS AND STATISTICS, MIAMI UNIVERSITY, OXFORD, OHIO 45056

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