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Ol'ga Aleksandrovna Ladyzhenskaya (March 7, 1922–January 12, 2004)

Ol'ga Aleksandrovna Ladyzhenskaya played an extraordinary role in the mathematical life of Leningrad–Saint Petersburg. Her influence stemmed from remarkable scientific achievements, personal charm, and civic virtue. The Editorial Board pay tribute to the memory of this great mathematician and personality. This issue of the journal consists of papers written by collaborators and former students of Ol'ga Aleksandrovna.

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 $^{^*}$ The American Mathematical Society scheme for transliteration of Cyrillic may be found at the end of index issues of *Mathematical Reviews*.

