

# St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

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Volume 20 Number 2 April 2009

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*A Translation of*

РОССИЙСКАЯ АКАДЕМИЯ НАУК

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(Formerly Leningrad Mathematical Journal)

*A translation of the Russian bimonthly*

Алгебра и анализ

“Наука”, С.-Петербургское отделение, 2008 г.

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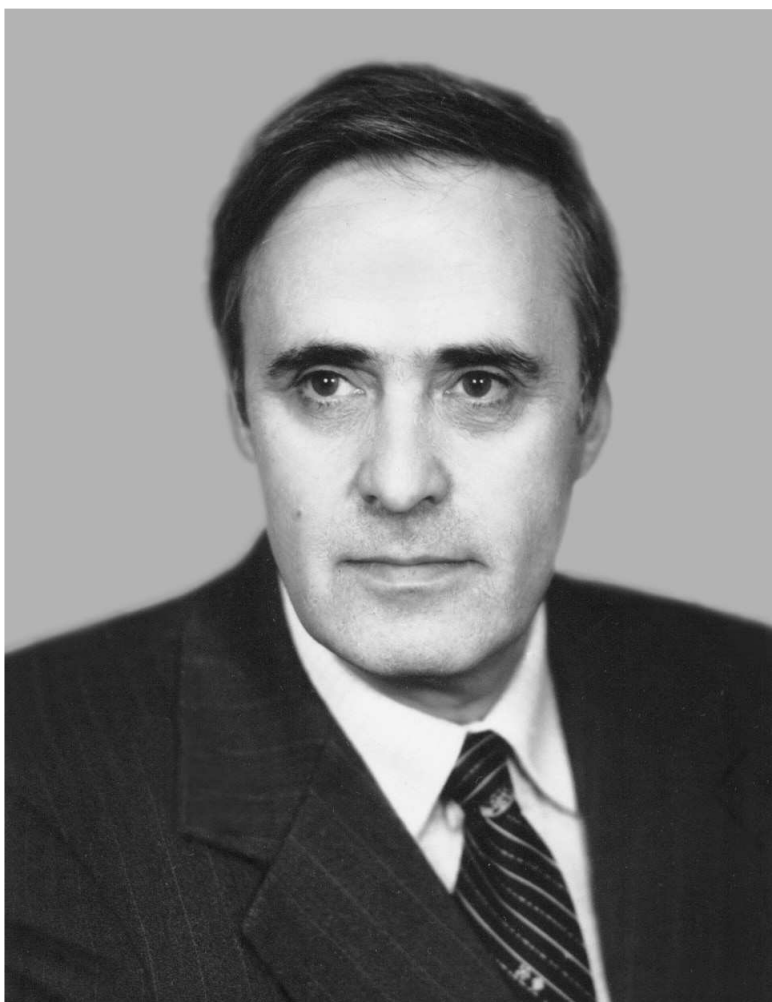
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The Editorial Board  
cordially congratulates  
**Mikhail Shlémovich Birman**  
on his 80th birthday.

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