

# St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

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Volume 22 Number 3 June 2011

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*A Translation of*

РОССИЙСКАЯ АКАДЕМИЯ НАУК

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ТОМ 22 № 3 2010



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Алгебра и анализ

“Наука”, С.-Петербургское отделение, 2010 г.

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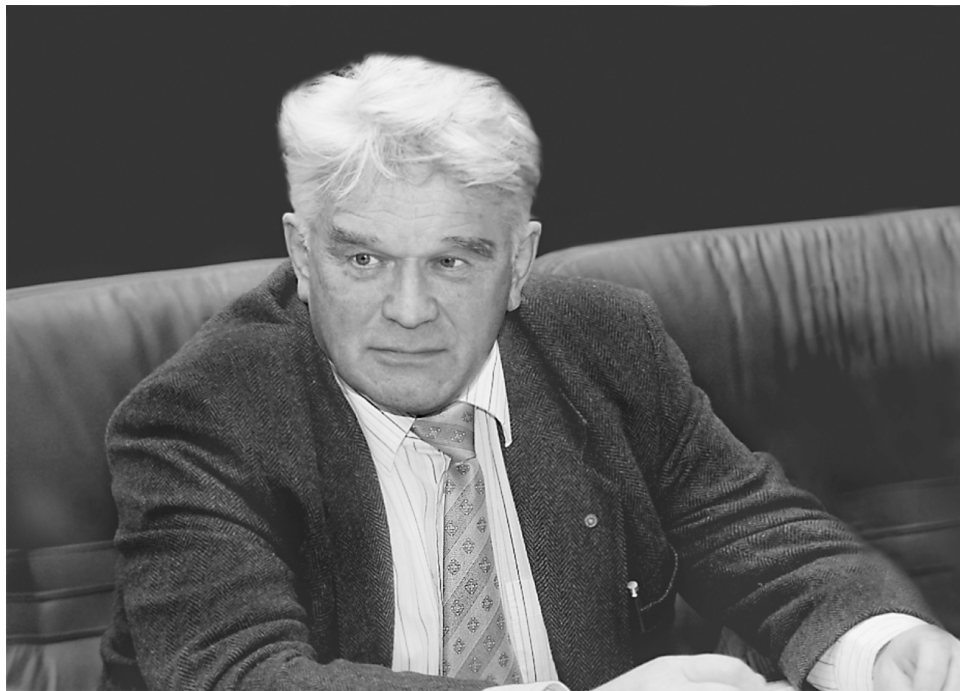
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The Editorial Board cordially congratulates  
Academician Ludvig Dmitrievich Faddeev,  
outstanding mathematician and theoretical physicist,  
on his 75th birthday.

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