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## CONTENTS

# **Research Papers**

J. Andersson, Optimal regularity and free boundary regularity for the Signorini	
problem	371
N. A. Vavilov and A. A. Semenov, Long root tori in Chevalley groups	387
S. A. Evdokimov and I. N. Ponomarenko, Schurity of S-rings over a cyclic	
group and generalized wreath product of permutation groups	431
A. Zhukova, Morse index of a cyclic polygon. II	461
S. O. Ivanov, The stable Calabi–Yau dimension of the preprojective algebra of	
type $\mathbf{L}_n$	475
G. Nebe and B. Venkov, On tight spherical designs	485
S. V. Poborchiĭ, Unique solvability of the Dirichlet problem for the equation	
$\Delta_p u = 0$ in the exterior of a paraboloid	493
A. L. Chistov, A bound for the degree of a system of equations determining the	
variety of reducible polynomials	513

# **RUSSIAN CONTENTS**\*

# СОДЕРЖАНИЕ

# Статьи

1
22
84
128
148
163
172
199

<sup>\*</sup>The American Mathematical Society scheme for transliteration of Cyrillic may be found at the end of index issues of *Mathematical Reviews*.

