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(Formerly Leningrad Mathematical Journal)

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Volume 25 Number 2 April 2014

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*A Translation of*

РОССИЙСКАЯ АКАДЕМИЯ НАУК

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Алгебра и анализ

“Наука”, С.-Петербургское отделение, 2013 г.

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