

St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

Volume 27 Number 3 June 2016

A Translation of

РОССИЙСКАЯ АКАДЕМИЯ НАУК

АЛГЕБРА

И

АНАЛИЗ

ТОМ 27 № 3 2015



American Mathematical Society

Providence, Rhode Island USA

ISSN 1061-0022 (print)

ISSN 1547-7371 (online)

ST. PETERSBURG MATHEMATICAL JOURNAL

(Formerly Leningrad Mathematical Journal)

A translation of the Russian bimonthly

Алгебра и анализ

“Наука”, С.-Петербургское отделение, 2015 г.

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The Editorial Board of “Algebra i Analiz”
cordially congratulates
Nina Nikolaevna Ural'tseva on her anniversary.

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1061-0022(201606)27:3;1-E