

# St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

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Volume 29 Number 2 April 2018

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*A Translation of*

РОССИЙСКАЯ АКАДЕМИЯ НАУК

АЛГЕБРА  
И  
АНАЛИЗ

ТОМ 29 № 2 2017



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(Formerly Leningrad Mathematical Journal)

*A translation of the Russian bimonthly*

Алгебра и анализ

“Наука”, С.-Петербургское отделение, 2017 г.

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This issue is dedicated to the memory of Vladimir Savel'evich Buslaev (1937–2012), a brilliant mathematician who would have reached the age of 80 in 2017.

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