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Volume 29 Number 3 June 2018

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РОССИЙСКАЯ АКАДЕМИЯ НАУК

# АЛГЕБРА и АНАЛИЗ

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"Наука", С.-Петербургское отделение, 2017 г.

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 $<sup>^*</sup>$ The American Mathematical Society scheme for transliteration of Cyrillic may be found at the end of index issues of  $Mathematical\ Reviews$ .



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