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ТОМ 30 № 2 2018



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Алгебра и анализ

“Наука”, С.-Петербургское отделение, 2018 г.

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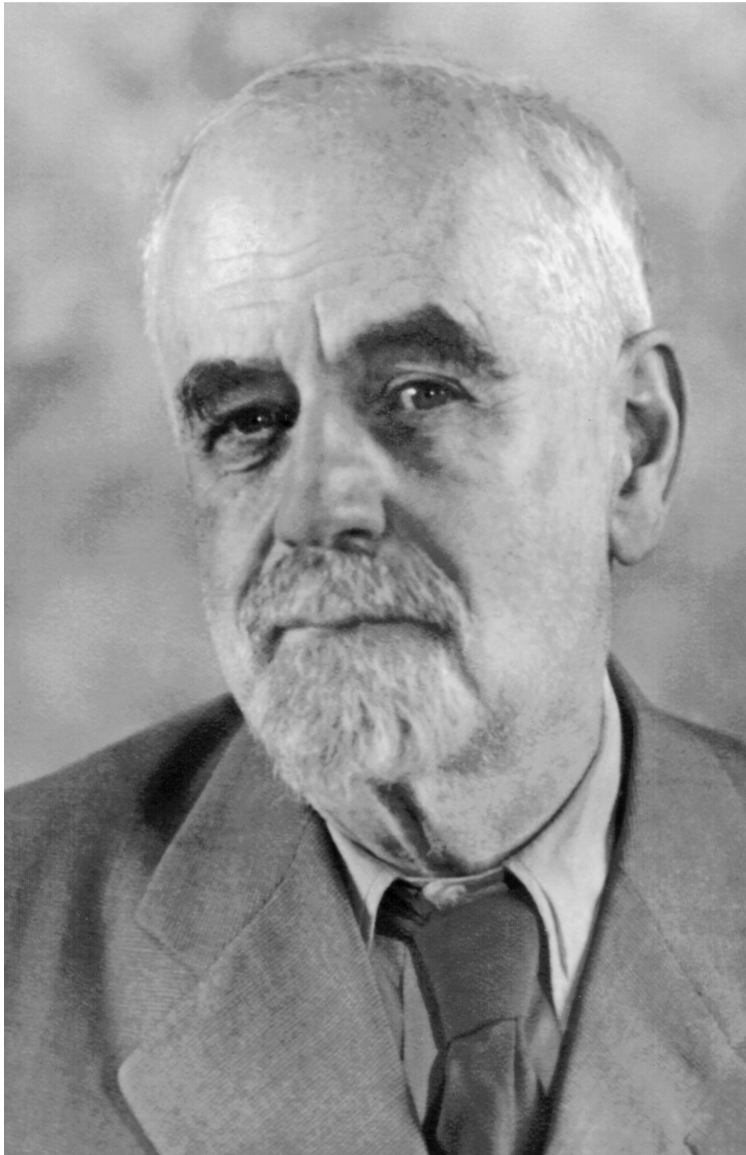
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Vladimir Ivanovich Smirnov (1887–1974)

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