

# St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

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Volume 31 Number 1 February 2020

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*A Translation of*

РОССИЙСКАЯ АКАДЕМИЯ НАУК

АЛГЕБРА  
И  
АНАЛИЗ

ТОМ 31 № 1 2019



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# ST. PETERSBURG MATHEMATICAL JOURNAL

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*A translation of the Russian bimonthly*

Алгебра и анализ

“Наука”, С.-Петербургское отделение, 2019 г.

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## CONTENTS

### Research Papers

<b>M. I. Belishev and A. F. Vakulenko</b> , On algebras of harmonic quaternion fields in $\mathbb{R}^3$ .....	1
<b>D. V. Korikov</b> , Asymptotics of eigenvalues of the Maxwell system in a domain with small cavities .....	13
<b>R. Macaitienė</b> , Some relations between zeros and universality of the Riemann zeta-function .....	53
<b>I. Nekrasov and G. Panina</b> , Geometric presentation for the cohomology ring of polygon spaces .....	59
<b>V. Nesterov</b> , Subsystem subgroups of the group of type $F_4$ generated by short root subgroups .....	69
<b>S. Yu. Orevkov</b> , Separating semigroup of hyperelliptic curves and of genus 3 curves .....	81
<b>D. A. Polyakova</b> , General solution of the homogeneous convolution equation in spaces of ultradifferentiable functions .....	85
<b>M. Seto and S. Suda</b> , Gram matrices of reproducing kernel Hilbert spaces over graphs IV. (Quadratic inequalities for graph Laplacians) .....	107
<b>B. N. Khabibullin and A. V. Shmeleva</b> , Balayage of measures and subharmonic functions to a system of rays. I. The classical case .....	117
<b>D. V. Khlopin</b> , Asymptotics of values in dynamic games on large intervals ....	157
<b>A. Tsybyshev</b> , A step towards the mixed-characteristic Grothendieck–Serre conjecture .....	181

## RUSSIAN CONTENTS\*

### СОДЕРЖАНИЕ

#### Статьи

<i>Белишев М. И., Вакуленко А. Ф.</i> Об алгебрах гармонических кватернионных полей в $\mathbb{R}^3$ . . . . .	1
<i>Кориков Д. В.</i> Асимптотика собственных значений системы Максвелла в области с малыми полостями . . . . .	18
<i>Macaïtiéné R.</i> Some relations between zeros and universality of the Riemann zeta-function . . . . .	72
<i>Nekrasov I., Panina G.</i> Geometric presentation for the cohomology ring of polygon spaces . . . . .	80
<i>Нестеров В.</i> Подсистемные подгруппы группы типа $F_4$ , порожденные короткими корневыми подгруппами . . . . .	92
<i>Орехов С. Ю.</i> Разбивающая полугруппа гиперэллиптических кривых и кривых рода 3. . . . .	108
<i>Полякова Д. А.</i> Общее решение однородного уравнения свертки в пространствах ультрадифференцируемых функций . . . . .	114
<i>Seto M., Suda S.</i> Gram matrices of reproducing kernel Hilbert spaces over graphs IV. (Quadratic inequalities for graph Laplacians) . . . . .	143
<i>Хабибуллин Б. Н., Шмелёва А. В.</i> Выметание мер и субгармонических функций на систему лучей. I. Классический случай. . . . .	156
<i>Хлопин Д. В.</i> Об асимптотиках цен в динамических играх на больших промежутках. . . . .	211
<i>Цыбышев А.</i> Один шаг в сторону неравнохарактеристической гипотезы Гротендика–Серра . . . . .	246

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