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N. N. Ural′tseva at the city seminar on mathematical physics, 1968.

This issue, like the preceding one, is dedicated to the anniversary of Nina Nikolaevna Ural′tseva, an outstanding St. Petersburg mathematician, a great expert in partial differential equations and calculus of variations.

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