

# Theory of Probability and Mathematical Statistics

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Number 90 2015

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*A Translation of*

ТЕОРІЯ  
ЙМОВІРНОСТЕЙ ТА  
МАТЕМАТИЧНА  
СТАТИСТИКА

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ТЕОРІЯ ЙМОВІРНОСТЕЙ ТА МАТЕМАТИЧНА СТАТИСТИКА

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## CONTENTS

<b>R. Abu-Shanab and A. Yu. Veretennikov</b> , On asymptotic Borovkov–Sakhanenko inequality with unbounded parameter set .....	1
<b>O. L. Banna, Yu. S. Mishura, and S. V. Shklyar</b> , Approximation of a Wiener process by integrals with respect to the fractional Brownian motion of power functions of a given exponent .....	13
<b>Iu. V. Ganychenko</b> , An estimate of the rate of convergence of a sequence of additive functionals of difference approximations for a multidimensional diffusion process .....	23
<b>V. V. Golomozyĭ</b> , An inequality for the coupling moment in the case of two inhomogeneous Markov chains .....	43
<b>T. Gorbach</b> , Estimation of parameters of a mixture of two symmetric distributions from a biased sample .....	57
<b>O. V. Doronin</b> , Lower bound for a dispersion matrix for the semiparametric estimation in a model of mixtures .....	71
<b>O. V. Ivanov and K. K. Moskvichova</b> , Stochastic asymptotic expansion of correlogram estimator of the correlation function of random noise in nonlinear regression model .....	87
<b>D. V. Koroliouk</b> , Two component binary statistical experiments with persistent linear regression .....	103
<b>G. L. Kulinich, S. V. Kushnirenko, and Yu. S. Mishura</b> , Asymptotic behavior of the martingale type integral functionals for unstable solutions to stochastic differential equations .....	115
<b>A. V. Logachov</b> , Large deviations for solutions of one dimensional Itô equations .....	127
<b>V. I. Masol and S. Ya. Slobodyan</b> , Normal limiting distribution of the normalized number of extraneous solutions of a compatible system of nonlinear random equations over the field GF(2) .....	139
<b>I. K. Matsak</b> , On a single-server queueing system with refusal .....	153
<b>S. A. Mel’nik</b> , Comparison theorem for solutions of parabolic stochastic equations with an absorber .....	161
<b>M. G. Semeĭko</b> , Moment measures of mixed empirical random point processes and marked point processes in compact metric spaces. 2 .....	175
<b>N. V. Troshki</b> , Accuracy and reliability of a model for a Gaussian homogeneous and isotropic random field in the space $L_p(\mathbb{T})$ , $p \geq 1$ .....	183
<b>Ya. M. Khusanbaev</b> , Convergence of a sequence of nearly critical branching processes with immigration .....	201
<b>Andriy Yurachkivsky</b> , Convergence of stochastic integrals to a continuous local martingale with conditionally independent increments .....	207

## UKRAINIAN CONTENTS\*

<i>R. Abu-Shanab, A. Yu. Veretennikov</i> On asymptotic Borovkov–Sakhanenko inequality with unbounded parameter set	1
<i>O. Л. Банна, Ю. С. Мішура, С. В. Шкляр</i> Наближення вінерівського процесу інтегралами від степеневих функцій зі сталим показником за дробовим броунівським рухом	13
<i>Ю. В. Ганиченко</i> Оцінка швидкості збіжності послідовності адитивних функціоналів від різницевих апроксимацій багатомірної дифузійної процесу	22
<i>В. В. Голомозий</i> Нерівності для моменту склеювання двох неоднорідних ланцюгів Маркова	39
<i>Т. Горбач</i> Оцінювання параметрів суміші двох симетричних розподілів за зміщеною вибіркою	52
<i>О. В. Доронін</i> Нижня межа матриці розсіяння для семіпараметричного оцінювання у моделі суміші	64
<i>О. В. Іванов, К. К. Москвичова</i> Стохастичний асимптотичний розклад корелограмної оцінки коваріаційної функції випадкового шуму в нелінійній моделі регресії	77
<i>Д. В. Корольок</i> Двокомпонентні бінарні статистичні експерименти з наполегливою лінійною регресією	91
<i>Г. Л. Кулініч, С. В. Кушніренко, Ю. С. Мішура</i> Асимптотична поведінка інтегральних функціоналів мартингального типу від нестійких розв'язків стохастичних диференціальних рівнянь	102
<i>А. В. Логачѳв</i> Большие уклонения для решений одномерных уравнений Ито	113
<i>В. І. Масол, С. Я. Слободян</i> Нормальний граничний розподіл нормованого числа сторонніх розв'язків сумісної системи нелінійних випадкових рівнянь над полем $GF(2)$	123
<i>І. К. Мацак</i> Про однолінійну систему масового обслуговування з втратами	135
<i>С. А. Мельник</i> Сравнение решений стохастических параболических уравнений с поглотителем	142
<i>М. Г. Семейко</i> Моментні міри змішаних емпіричних випадкових точкових процесів і маркованих точкових процесів в компактних метричних просторах. 2	155

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<i>Н. В. Трошкі</i>	Точність та надійність моделі гауссового однорідного та ізотропного випадкового поля у просторі $L_p(\mathbb{T})$ , $p \geq 1$	161
<i>Я. М. Хусанбаев</i>	О сходимости последовательности почти критических ветвящихся процессов с иммиграцией	177
<i>Андрій Юрачківський</i>	Збіжність стохастичних інтегралів до неперервного локального мартингала з умовно незалежними приростами	182







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