

Theory of Probability and Mathematical Statistics

Number 98 2019

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МАТЕМАТИЧНА
СТАТИСТИКА

ВИПУСК 98 2018



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